

**UNIVERSITY OF CRAIOVA**  
**Faculty of Mathematics and Computer Science**  
**Department of mathematics**  
**Fundamental domain : Exact sciences**  
**Domain: Mathematics**  
**Master: Applied mathematics**  
**Form: day classes**  
**Duration of studies: 2 years**  
**Approved with academic year 2008-2009**

## **Evolution equations Syllabus**

**Course coordinator:** Prof. dr. Micu Sorin  
**Code:** MA123  
**Second Cycle:** MASTER  
First year, Second Semester, Course 28 hours, Seminar 28 hours  
**No of credits:** 6  
**Domain:** Mathematics  
**Type :** compulsory  
**Category:** speciality

**Objectives:** We study the existence, uniqueness, regularity and asymptotic behavior of the solutions of linear and semi-linear equations of evolution.

**Necessary background:** Functional analysis, Partial differential equations

**Evaluation :** Exam (E)

### **Contents:**

Introduction

Unbounded operators. Semigroups. Hille-Yosida Theorem. Classical and weak solutions of the homogeneous and nonhomogeneous equations of evolution.

Diagonalizable operators in Hilbert space. Spaces scale of sequences and functions. Fundamental properties. Bounded perturbations.

Semi-linear heat equation: local and global existence. Finite time blowup.

Semi-linear wave equation: local and global existence. Finite time blowup.

Asymptotic behavior of solutions of evolution equations. Bounded solutions. Invariance principle of LaSalle.

Introduction in control theory

### **References:**

H. Brezis: *Analyse fonctionnelle: Théorie et applications*, Masson, Paris, 1983.

V. Barbu: *Probleme la limită pentru ecuațiile cu derivate parțiale*, Ed. Academiei, București, 1993.

T. Cazenave și A. Haraux: *Introduction aux problèmes d'évolution semi-linéaires*, Ellipses, Paris, 1990.