

Bifurcations of continuous dynamical systems. Applications in economics and biology, Universitaria, Craiova, 2006 (Romanian), 270 p.

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